

Unit 9 (Chapter 11): Limits**11.3 More on Limits**

Target 9A: Evaluate a limit of a function algebraically

Target 9D: Calculate one-sided limits and two-sided limits

Review of Prior Concepts

1. $\lim_{x \rightarrow \infty} \left(\frac{x^2 - 4}{x+2} \right)$

2. $\lim_{x \rightarrow -\infty} \left(\frac{x^2 - 4}{x+2} \right)$

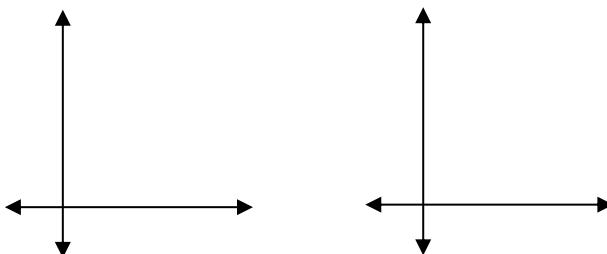
3. $\lim_{x \rightarrow 2} \left(\frac{x^2 - 4}{x+2} \right)$

More Practice**Limits at Infinity**<https://www.mathsisfun.com/calculus/limits-infinity.html><https://www.khanacademy.org/math/ap-calculus-ab/infinite-limits-ab/limits-at-infinity-ab/v/limits-and-infinity><http://www.shmoop.com/precalculus-limits/limits-infinity.html><https://youtu.be/wBYr-58mc5E><https://youtu.be/75xO9xy7TTQ><https://youtu.be/FVJNuukADeQ>**3 Methods for Evaluating Limits**

①

②

③

What does $\lim_{x \rightarrow c} f(x) = L$ mean?As x approaches (but doesn't reach) c from either side, then $f(x)$ becomes arbitrarily close to L .

Evaluate Limits Analytically/Algebraically

- Replace the value of c for x (if possible)

Examples:

1. Find: $\lim_{x \rightarrow 2} (x^3 - 2x)$

2. Find: $\lim_{x \rightarrow 1} 4x$

3. Find: $\lim_{x \rightarrow a} (x^3 + 4x)$

4. Find: $\lim_{x \rightarrow -1} \frac{x^2 - 1}{x - 1}$

5. Find: $\lim_{x \rightarrow 1} \frac{x^2 - 1}{x - 1}$

6. Find: $\lim_{x \rightarrow 3} \frac{x^2 + 2x - 15}{x^2 - 9}$

7. Find: $\lim_{x \rightarrow 5} \sqrt{16 - x^2}$

8. Find: $\lim_{x \rightarrow 1} \frac{\sqrt{x+3}-2}{x-1}$

Find: a) $\lim_{x \rightarrow 0} \frac{\sin x}{x}$ b) $\lim_{x \rightarrow 0} \frac{\sin 2x}{2x}$ c) $\lim_{x \rightarrow 0} \frac{\sin 10x}{10x}$

$$\lim_{x \rightarrow 0} \frac{\sin ax}{ax} = \quad , \text{ where } a \text{ is a constant (#)}$$

Examples:

1. $\lim_{x \rightarrow 0} \frac{\sin 4x}{x}$

2. $\lim_{x \rightarrow 0} \frac{\sin 3x}{2x}$

3. $\lim_{x \rightarrow 0} \frac{3x + \sin x}{x}$

4. $\lim_{x \rightarrow 0} \frac{\sin^2 x}{x^3 - 2x^2}$

More Practice

Limits Analytically

<http://www.ck12.org/book/CK-12-Precalculus-Concepts/section/14.4/>

<http://www.ck12.org/book/CK-12-Precalculus-Concepts/section/14.5/>

<http://precalculus.flippedmath.com/151-limits-analytically.html>

<http://www.barrington220.org/cms/lib8/IL01001296/Centricity/Domain/321/1.3%20D1%20Ans.pdf>

<https://youtu.be/-gjURkNuh9o>

<https://youtu.be/MspCIN-r8C0>

Homework Assignment

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