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Unit 2 (Chapter 2): Polynomial \& Rational Functions

### 2.3 Polynomial Functions of Higher Degree w/Modeling

Target 2A: Graph, Solve and Analyze Polynomial Functions

## Multiplicity of Zeros of Polynomials: Discovery Activity

1. Graph $f(x)=x(x-2)(x+2)(x-1)$ on a graphing calculator
a. What are the zeros of the function?
b. For what value(s) of $x$ does the graph of the function cross the $x$-axis?
c. For what value(s) of $x$ does the graph of the function touch but not cross the $x$-axis?
d. What degree is the polynomial?
2. Graph each function in the table. For each function, answer the questions asked in Question 1. Use the table below to record your results.

| $\#$ | Function | Zeros | Cross | Touch | Degree |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $f(x)=(x+1)^{2}(x-2)(x-1)$ |  |  |  |  |
| $\mathbf{2}$ | $f(x)=(x-2)^{2}(x+1)(x-1)$ |  |  |  |  |
| $\mathbf{3}$ | $f(x)=(x+2)^{2}(x-1)^{2}$ |  |  |  |  |
| $\mathbf{4}$ | $f(x)=(x+1)^{3}(x-1)(x-2)$ |  |  |  |  |
| $\mathbf{5}$ | $f(x)=(x-2)^{2}(x-1)(x+1)^{2}$ |  |  |  |  |

3. How are the zeros of a polynomial function related to the factors of a polynomial function?
4. How do the exponents in each term in the factored form of the polynomial function affect its graph? (Notice: When does the graph cross the $x$-axis and when does the graph touch the $x$-axis?)
5. When a polynomial has a repeated linear factor, it has a multiple zero.
a. Write the factored form of a polynomial function that crosses the $x$-axis at $x=-2$ and $x=5$ and touches the $x$-axis at $x=3$.
b. Which of the zeros of the function must have a multiplicity greater than 1? Explain your reasoning.
6. Write two additional polynomial functions that meet the same conditions as described in Question 5.

Explain what is different from your function in Question 5, and how you determined your polynomial functions.

## Summary of Multiplicity of Zeroes of Polynomial Functions



Odd multiplicity $\rightarrow$ the graph crosses $x$-axis @
Even multiplicity $\rightarrow$ the graph touches $x$-axis @
$x=c$
ex: $f(x)=(x-2)^{3}$
ex: $f(x)=(x-2)^{4}$

State the degree and list the zeros of the polynomial function. State the multiplicity of each zero and whether the graph crosses or touches the $x$-axis at the corresponding $x$-intercept.
Then sketch the graph of the polynomial function by hand.

## Example 1: <br> $f(x)=x(x+4)^{2}(x-6)$

Example 2:
$g(x)=(x-5)^{3}(x+6)(x+2)^{2}$

## Example 3:

Write a polynomial function that has a zero with multiplicity of 2 at $x=3$ and a zero with multiplicity of 1 at $x=-5$. Then sketch the graph of the polynomial by hand.

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    More Practice
Multiplicities of Zeroes in Polynomials
http://www.onemathematicalcat.org/Math/Precalculus_obj/multZeroes.htm
http://stem.utm.edu/cats/index.php/Zeros_and_multiplicities
http://www.coolmath.com/algebra/22-graphing-polynomials/06-zeros-multiplicities-01
https://www.youtube.com/watch?v=XmqJx4ujBr0
https://www.youtube.com/watch?v=B9SNJXvP t0
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## Homework Assignment <br> p. 193 \#29,32,37,41,51,53,65,73,74

