

## 5.1 Fundamental Trig Identities

Target 6A: Verify, evaluate, and apply trigonometric identities and formulas

*Review of Prior Concepts*

If  $\sin \theta = 0.57$ , then  $\sin(\pi - \theta) = ?$

### Reciprocal Identities

$$\sin \theta = \frac{1}{\text{_____}}$$

$$\csc \theta = \frac{1}{\text{_____}}$$

$$\cos \theta = \frac{1}{\text{_____}}$$

$$\sec \theta = \frac{1}{\text{_____}}$$

$$\tan \theta = \frac{1}{\text{_____}}$$

$$\cot \theta = \frac{1}{\text{_____}}$$

### Quotient Identities

$$\tan \theta = \text{_____}$$

$$\cot \theta = \text{_____}$$

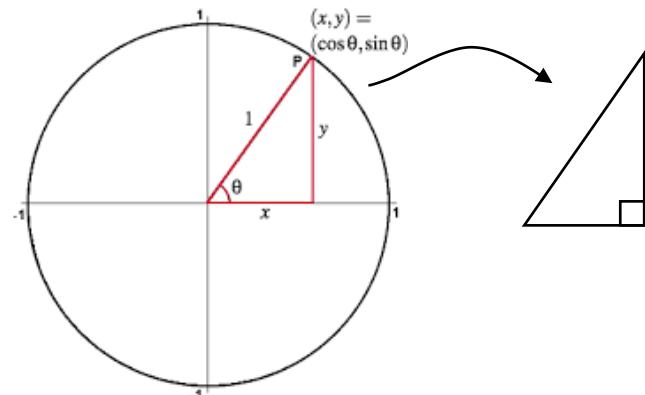
### Examples

**Simplify.**

a)  $\cot x \tan x$

b)  $\frac{\sin b}{\tan b}$

### Pythagorean Identities



*Examples*

a) Use Pythagorean Identities to find  $\sec \theta$  and  $\csc \theta$   
if  $\tan \theta = 3$  and  $\cos \theta > 0$ .

b) Simplify  $\frac{\sin^2 \alpha + \tan^2 \alpha + \cos^2 \alpha}{\sec \alpha}$

*Cofunction Identities*

$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta \quad \cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$

$$\tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta \quad \cot\left(\frac{\pi}{2} - \theta\right) = \tan \theta$$

$$\sec\left(\frac{\pi}{2} - \theta\right) = \csc \theta \quad \csc\left(\frac{\pi}{2} - \theta\right) = \sec \theta$$

*Odd-Even Identities*

$$\sin(-x) = -\sin x \quad \csc(-x) = -\csc x$$

$$\cos(-x) = \cos x \quad \sec(-x) = \sec x$$

$$\tan(-x) = -\tan x \quad \cot(-x) = -\cot x$$

*Examples*

a) If  $\tan\left(\frac{\pi}{2} - \theta\right) = -5.326$ , find  $\cot \theta$ .

b) Simplify  $\sec(-x) \cos(-x)$

**More Practice****Fundamental Trig Identities**

<http://www.intmath.com/analytic-trigonometry/1-trigonometric-identities.php>

<http://www.mathguide.com/lessons2/TrigExpress.html>

<http://www.purplemath.com/modules/proving.htm>

<https://www.youtube.com/watch?v=CsfHFZL345M>

<https://www.youtube.com/watch?v=I4mcja8abDc>

**Homework Assignment**

p.410 #3,5,9,13,14,15,17,19,23