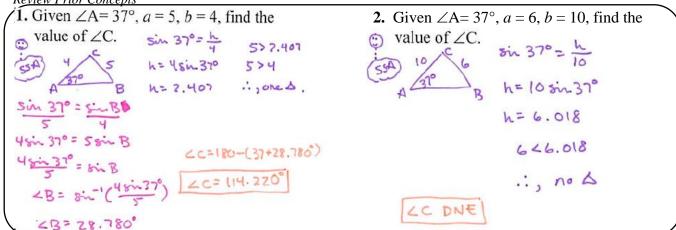
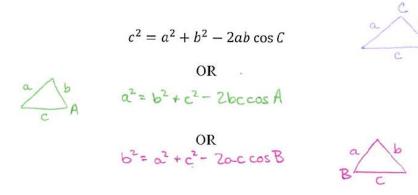
5.6 The Law of Cosines

Target 6D: Use Law of Sines and Law of Cosines to solve triangles

Review Prior Concepts



Law of Cosines

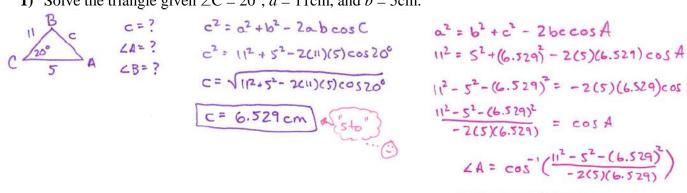


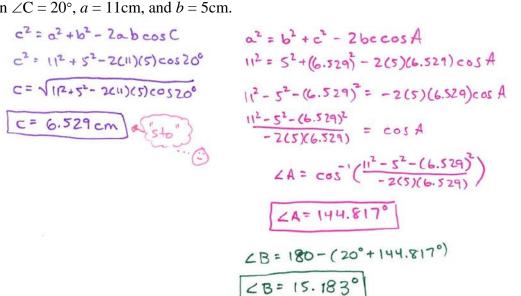
⊃With what given conditions can Law of Cosines be used?



Examples

1) Solve the triangle given $\angle C = 20^{\circ}$, a = 11cm, and b = 5cm.

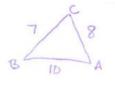




Unit 6 (Chapter 5): Analytic Trigonometry

Pre-Calculus

2) Solve the triangle given a = 7, b = 8, and c = 10.



$$c^2 = a^2 + b^2 - 2ab \cos C$$
 $10^2 = 7^2 + 8^2 - 2(7)(8) \cos C$
 $100 = 113 - 112 \cos C$
 $-13 = -112 \cos C$
 $\frac{13}{112} = \cos C$
 $2c = \cos^{-1}(\frac{13}{112})$
 $3c = 2c + b^2 - 2ab \cos C$
 $3c = 13 - 112 \cos C$

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$

$$7^{2} = 8^{2} + 16^{2} - 2(8)(10)\cos A$$

$$7^{2} - 8^{2} - 16^{2} = -2(8)(10)\cos A$$

$$\frac{7^{2} - 8^{2} - 16^{2}}{-2(8)(10)} = \cos A$$

$$\angle A = \cos^{-1}(\frac{7^{2} - 8^{2} - 16^{2}}{-2(8)(10)})$$

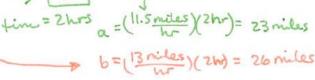
$$\angle A^{2} + 44.049^{\circ}$$

$$\angle B = 180 - (83.335^{\circ} + 44.049^{\circ})$$

$$\angle B = 52.617^{\circ}$$

Applications

Two ships leave port at 4 p.m. One is headed at a bearing of N 38 E and is traveling at 11.5 miles per hour. The other is traveling 13 miles per hour at a bearing of S 47 E. How far apart are they when dinner is served at 6 p.m.?

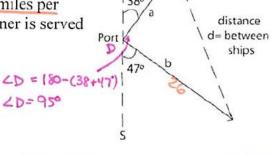


$$d^{2} = a^{2} + b^{2} - 2ab \cos D$$

$$d^{2} = 23^{2} + 26^{2} - 2(23)(26) \cos 95^{\circ}$$

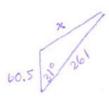
$$d^{2} = \sqrt{23^{2} + 26^{2} - 2(23)(26) \cos 95^{\circ}}$$

$$d^{2} = 36.183$$



The two ships are 36.183 miles apart when dinner is served

2) On a baseball field, the pitcher's mound is 60.5 feet from home plate. During practice, a batter hits a ball 261 feet at an angle of 31° to the right of the pitcher's mound. The right fielder catches the ball and throws it to the pitcher. How far does the right fielder throw the ball?

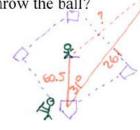


$$x^{2} = 60.5^{2} + 261^{2} - 2(60.5)(261)\cos 31^{6}$$

$$x = \sqrt{60.5^{2} + 261^{2} - 2(60.5)(261)\cos 31^{6}}$$

x= 211.45

The right fielder throws the ball 211.45 ft



More Practice

Law of Cosines

https://www.mathsisfun.com/algebra/trig-cosine-law.html

http://www.mathwarehouse.com/trigonometry/law-of-cosines-formula-examples.php

https://www.khanacademy.org/math/geometry/hs-geo-trig/hs-geo-law-of-cosines/e/law_of_cosines

https://www.youtube.com/watch?v=ZElOxG7_m3c

https://www.youtube.com/watch?v=ZElOxG7_m3c

https://www.youtube.com/watch?v=QkpDJaze31k

Homework Assignment

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