## DATE:

## Unit 10 (Chapter 6): Parametric \& Polar

Pre-Calculus 2017-2018

### 6.3 Parametric Equations Practice

Target 10A: Define and graph parametric equations
Target 10B: Perform parametric/rectangular conversions

1. a) Make a table of values and sketch the curve, indicating the direction of your graph.

| $x(t)=1-2 t, y(t)=$ |  |  |
| :---: | :---: | :---: |
| $t$ | $x$ | $y$ |
| -3 | 7 | 5 |
| -2 | 5 | 4 |
| -1 | 3 | 3 |
| 0 | 1 | 2 |
| 1 | -1 | 1 |
| 2 | -3 | 0 |
| 3 | -5 | -1 |


b) Eliminate the parameter of the equations above and give the resulting rectangular equation.

2. a) Make a table of values and sketch the curve, indicating the direction of your graph.

$$
\begin{align*}
& x(t)=t+2 \\
& y(t)=\frac{4}{t}
\end{align*}
$$


b) Eliminate the parameter of the equations above and give the resulting rectangular equation.

$$
\begin{aligned}
& x=t+2 \\
& x-2=t
\end{aligned} \quad \begin{aligned}
& y=\frac{4}{t} \\
& y=\frac{4}{x-2}, \text { where } x \geq 4 \text { and } 0<y \leq 2 .
\end{aligned}
$$

Notice the restriction $t \geq 2$.
$x(2)=2+2=4$, so $x \geq 4$.
$y(2)=\frac{4}{2}=2$, so $0<y \leq 2$.
3. : $^{-}$Using your graphing calculator, graph the parametric equations:

$$
x(t)=\cos t, \quad y(t)=\sin t
$$

What does the graph look like? Circle
4. ${ }^{-2}$ Using your graphing calculator, graph the parametric equations:

$$
x(t)=2 \sin t, \quad y(t)=4 \cos t
$$

What does the graph look like? Ellipse

## Converting from Parametric Trig Equations to Rectangular

Determining a Rectangular Equation for Given Parametric Trig Equations

- Use a trig identity to help convert (i.e., $\sin ^{2} \theta+\cos ^{2} \theta=1$ )
- Solve the parametric equations for the trig functions in the trig identity \& sub into trig identity.
- Rewrite the rectangular equation into a recognizable equation.

Example 1: Write the parametric equations in rectangular form.

$$
x(t)=\frac{1}{2} \cos t, \quad y(t)=\frac{1}{2} \sin t
$$



Example 2: Write the parametric equations in rectangular form.

$$
x(t)=2 \sin t, \quad y(t)=4 \cos t
$$



Example 3: Write the parametric equations in rectangular form.

$$
x(t)=3 \cos t-1, \quad y(t)=2 \sin t+4
$$



