8.1, 8.2 & 8.3 Parabolas, Ellipses & Hyperbolas

Target 4A/4C/4E: Investigate the geometric properties of parabolas/ellipses/hyperbolas Target 4B/4D/4F: Derive the standard equation of a parabola/ellipse/hyperbola and graph given two or three criteria

Practical Applications of Conic Sections

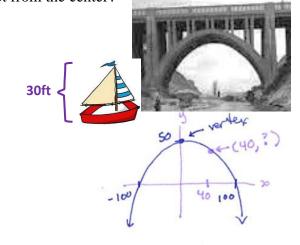
1. The parabolic arch shown in the figure is 50 feet above water at the center and 200 feet wide at the base. Will a boat that is 30 feet tall clear the arch 40 feet from the center?

vertex: (0,50)
point: (100,0) + (-100,0) (x-h)=4p(y-K) (x-0)2=4p(y-50) = sub in vertex x2 = 4p(y-50) + Sulo in point (100,0) 100 = 4p (0-50) solve for p 10000 = -200p -50 = P x2= 4(-50) (4-50) x2= -200 (y-50) = use equation to 1600 = -200y + 10000

-8400 = -200y height of biology 40ft 42ft.

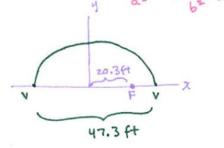
Clear the arch 40ft From center is 42ft.

40ft From the center is 42ft.



2. The Whispering Gallery in the Museum of Science and Industry in Chicago is 47.3 feet long. The distance form the center of the room to the foci is 20.3 feet. Find an equation that describes the shape of the room. How high is the room at its center?





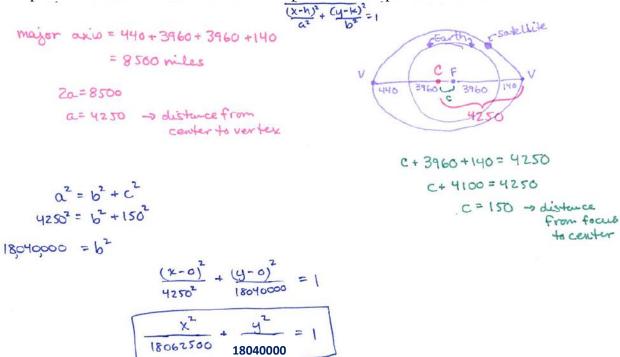
center to focus => c= 20.3

$$a^{3} + b^{2} + c^{2}$$
 $(23.65)^{2} = b^{2} + (20.3)^{2}$
 $12.134 = b$
The room is 12.134 ft tall

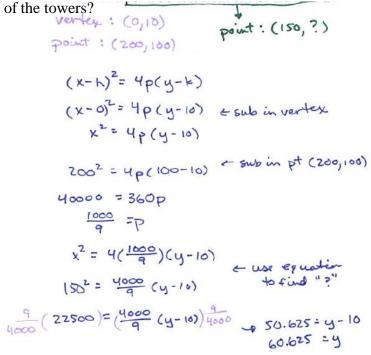
$$\frac{(x-0)^{2}}{23.65^{2}} + \frac{(y-0)^{2}}{12.134^{2}} = 1$$

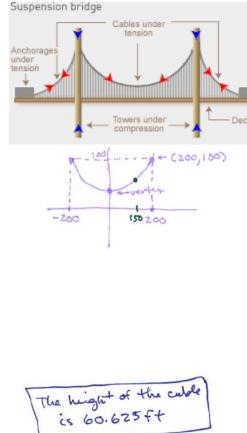
$$\frac{x^{2}}{559.3225} + \frac{y^{2}}{147.2325} = 1$$

3. A satellite is in elliptical orbit around the earth with the center of the Earth at one focus. The distance of the satellite from the Earth varies between 140 mi and 440 mi. Assume the Earth is a sphere with radius 3960 miles. Find an equation for the path of the satellite.



4. The towers of a suspension bridge are 400 feet apart and 100 feet high. Cables are at a height of 10 feet between the towers. Assuming the *x*-axis is the road and the *y*-axis is the center of the bridge, write an equation for the parabola. What is the height of the cable at a point 50 feet from one of the towers?





5. On the sidelines of each of its televised football games, the FBTV network uses a parabolic reflector with a microphone at the reflector's focus to capture the conversations among players on the field. If the parabolic reflector is 3 ft across and 1 ft deep, where should the microphone by placed?

Check the solution in OneNote.

More Practice

Applications of Conic Sections

http://www3.ul.ie/~rynnet/swconics/applications_of_conic_sections.htm

https://www.youtube.com/watch?v=6GVumC_Pie0

Solving Real-World Conic Section Problems

http://www.shelovesmath.com/precal/parametrics-and-conics/#ApplicationsofEllipses

http://www.purplemath.com/modules/ellipse4.htm

https://www.youtube.com/watch?v=lg4uuxI8leE

https://www.youtube.com/watch?v=umqE1LeluOo

https://www.youtube.com/watch?v=T2eHdLyD4P4

https://www.youtube.com/watch?v=DB7IPSWbmhM

Homework Assignment

p.579 #59,60,61; p.591 #53; p.601 #57