

Verbal Description

A racetrack is in the shape of an ellipse, 100 feet long and 50 feet wide. What is the width of the racetrack 10 feet from the vertex?

major axis = 100 ft
 minor axis = 50 ft

Algebraic

$$2a = 100$$

$$a = 50$$

$$2b = 50$$

$$b = 25$$

$$(40, y)$$

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\frac{x^2}{50^2} + \frac{y^2}{25^2} = 1$$

$$\frac{40^2}{50^2} + \frac{y^2}{25^2} = 1$$

$$\frac{16}{25} + \frac{y^2}{625} = 1$$

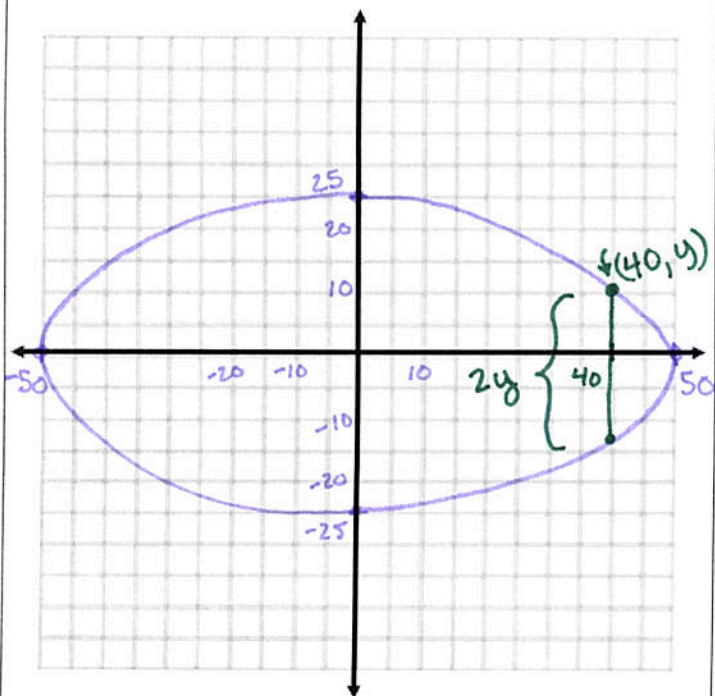
$$\frac{y^2}{625} = \frac{9}{25}$$

$$y^2 = 225$$

$$y = 15$$

$$\therefore, 2y = 30$$

Graphical



Written Conclusion

The width of the racetrack 10 feet from the vertex is 30 feet.