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## Calculator

1. An NFL place-kicker attempts a 40 yd field goal with an initial velocity of $70 \mathrm{ft} / \mathrm{sec}$ at a $45^{\circ}$ angle with the horizontal.
a) Model the motion of the football using parametric equations.
b) To make the field goal, the football will have to clear a 10 ft high crossbar. Will the kicker make the field goal if the kick sails "true"? By how much does the ball clear or fall short (vertically) of the crossbar?
c) What is the ball's maximum height above the field?
d) What is the ball's "hang time" (the total time the football is in the air)?
2. Find the rectangular coordinates of the polar coordinate point $\left(-2,-\frac{14 \pi}{5}\right)$. Approximate the coordinates to the nearest thousandth (three decimal places).
3. Find the intersection(s) of the following polar equations: $r=1+2 \cos \theta$ and $r=1+\sqrt{3}$
4. Complete the table for the polar equation $r=1+2 \sin \theta$ and sketch the graph at the points in the table (only on the interval $\frac{\pi}{2} \leq \theta \leq \frac{3 \pi}{2}$ ).

| $\boldsymbol{\theta}$ | $\frac{\pi}{2}$ | $\frac{3 \pi}{4}$ | $\pi$ | $\frac{7 \pi}{6}$ | $\frac{4 \pi}{3}$ | $\frac{3 \pi}{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{r}$ |  |  |  |  |  |  |



## Non-calculator

5. Use an algebraic method to eliminate the parameter $t$ and then identify the graph of the parametric curve.

$$
x=2 \sin t \quad y=2 \cos t, \quad \frac{\pi}{2} \leq t \leq \pi
$$

6. The graph of the parametric equations $x=t-2$ and $y=-3 t-2$ where $3 \leq t \leq 7$ is a line segment. Find the endpoints of this line segment.
7. Use an algebraic method to eliminate the parameter $t$ and then identify the graph of the parametric curve.

$$
x=2-3 t \quad y=-2 t-1
$$

8. Convert $\left(10,-\frac{\pi}{4}\right)$ from polar to rectangular coordinates.
9. Find two polar coordinate pairs for the point with rectangular coordinates $P(-2,2)$.
10. Convert each polar equation to rectangular form and identify the graph.
a) $r=\frac{1}{2} \sec \theta$
b) $r=3 \sin \theta-4 \cos \theta$
11. Transform each rectangular equation to a polar equation and identify the graph.
a) $x^{2}+y^{2}+6 y=0$
b) $(x-4)^{2}+y^{2}=16$
