

Honors Geometry
Practice

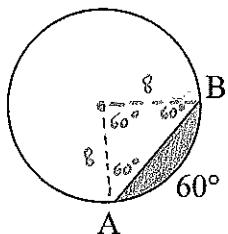
$$A_{\text{sector}} = \frac{m\widehat{AC}}{360} \cdot \pi r^2, \quad A_{\odot} = \pi r^2$$

$$A_{\text{seg}} = \frac{s\sqrt{3}}{4}, \quad A_{\text{reg poly}} = \frac{1}{2}ap$$

DATE: Key
Remember units²!

Find the area of each shaded region. All polygons are regular.

1.

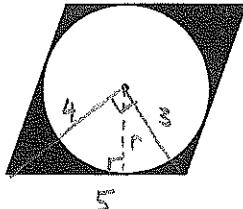


$$AB = 8$$

Area of segment of circle?

$$\begin{aligned} A_{\text{segment}} &= A_{\text{sector}} - A_{\text{seg}} \\ &= \frac{60}{360} \cdot \pi(8)^2 - \frac{(8)^2 \sqrt{3}}{4} \\ &= \frac{32}{3} \pi - 16\sqrt{3} \end{aligned}$$

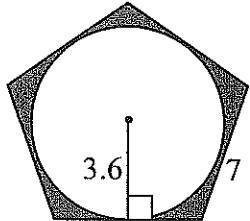
2.



rhombus
 $d_1 = 6$
 $d_2 = 8$

$$\begin{aligned} A_{\text{shaded}} &= A_{\text{rhombus}} - A_{\odot} \\ &= \frac{1}{2}(6)(8) - \pi\left(\frac{12}{5}\right)^2 \\ &= 24 - \frac{144\pi}{25} \\ &\approx 24 - 17.7 \end{aligned}$$

3.

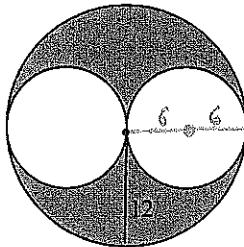


$$P = 5(7) = 35$$

$$A_{\text{shaded}} = A_{\text{reg. pent}} - A_{\odot}$$

$$\begin{aligned} &= \frac{1}{2}(3.6)(35) - \pi(3.6)^2 \\ &= 63 - 12.96\pi \end{aligned}$$

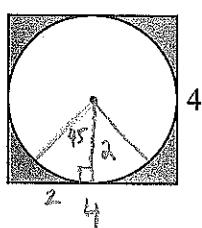
4.



$$A_{\text{shaded}} = A_{\text{large } \odot} - 2A_{\text{small } \odot}$$

$$\begin{aligned} &= \pi(12)^2 - 2(\pi(6)^2) \\ &= 144\pi - 2(36\pi) \\ &= 144\pi - 72\pi \\ &= 72\pi \end{aligned}$$

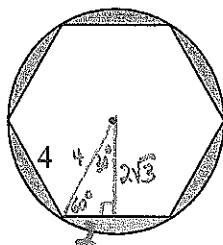
5.



$$A_{\text{shaded}} = A_{\text{sq}} - A_{\odot}$$

$$\begin{aligned} &= (4)^2 - \pi(2)^2 \\ &= 16 - 4\pi \end{aligned}$$

6.

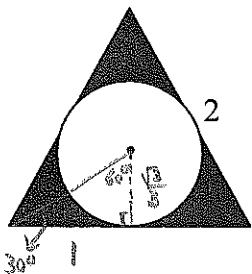


$$\begin{aligned} P &= 8(4) \\ &= 32 \end{aligned}$$

$$A_{\text{shaded}} = A_{\odot} - A_{\text{reg poly}}$$

$$\begin{aligned} &= \pi(4)^2 - \frac{1}{2}(2\sqrt{3}) \cdot 32 \\ &= 16\pi - 24\sqrt{3} \end{aligned}$$

7.



$$30 - 60 - 90$$

$$\downarrow \quad \downarrow \quad \downarrow$$

$$x \quad x\sqrt{3} \quad 2x$$

$$1 = x\sqrt{3}$$

$$\frac{1}{\sqrt{3}} = \frac{x\sqrt{3}}{x}$$

$$\frac{1}{\sqrt{3}} \cdot \frac{2}{\sqrt{3}} = \frac{\sqrt{3}}{3} \approx x$$

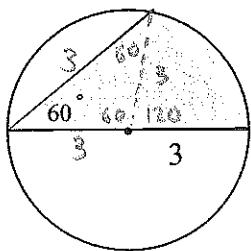
$$A_{\text{SHADED}} = A_{\star} - A_0$$

$$= \frac{(2)^2\sqrt{3}}{4} - \pi\left(\frac{2}{2}\right)^2$$

$$= \frac{4\sqrt{3}}{4} - 3\pi$$

$$= \sqrt{3} - \frac{3\pi}{4}$$

9.



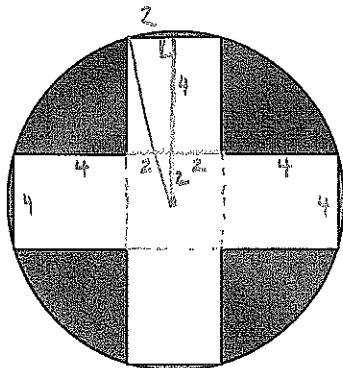
$$A_{\text{SHADED}} = A_{\star} + A_{\text{sector}}$$

$$= \frac{(3)^2\sqrt{3}}{4} + \frac{120}{360} \cdot \pi(3)^2$$

$$= \frac{9\sqrt{3}}{4} + \frac{1}{3}\pi(9)$$

$$= \frac{9\sqrt{3}}{4} + 3\pi$$

8.



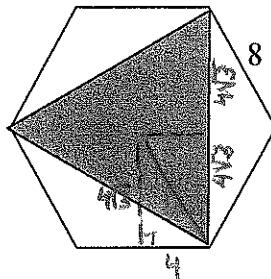
All 12 sides are 4 units
All angles are right

$$A_{\text{SHADED}} = A_0 - A_{\text{EL}}$$

$$= \pi(2\sqrt{10})^2 - 5(4)^2$$

$$= 40\pi - 80$$

10.



$$A_{\text{SHADED}} = \frac{(8\sqrt{3})^2\sqrt{3}}{4}$$

$$= \frac{192\sqrt{3}}{4}$$

$$= 48\sqrt{3}$$

ONE SIDE OF
SHADED Δ

$$= 8\sqrt{3}$$

