3.2. Honors Geometry

DATE:


Target 3B. Understand and apply the theorems and postulates sufficient to prove triangles congruent
Write a two-column proof.
Given: $A B \cong B C$

$$
\angle \mathrm{ABD} \cong \angle \mathrm{CBD}
$$

Prove: $\triangle A B D \cong \triangle C B D$

| Statement | Reason |
| :--- | :--- |
| (1) $\overline{A B} \cong \overline{B C}$ | Given |
| (3) $\angle A B D \cong \angle C B D$ | (2) Given |
| (3) $\overline{B D \cong B D}$ | (3) Reflexive Property |

(4) $\triangle A B D \cong \triangle C B D$
(4) SAS (Step 1,2,3)

Given: $B D \perp A C$

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$$
\angle \mathrm{ABD} \cong \angle \mathrm{CBD}
$$

Prove: $\triangle \mathrm{ABD} \cong \triangle C B D$

(5) $\overline{B D} \cong \overline{B D}$
(6) $\triangle A B O \cong \triangle C B D$

(2) If 2 seg 1 , then rt. $\angle s$.
(3) Rt. L's are $\cong$
(4) Given
(5) Ref lexive Propenty
(6) ASA (Step 4,5,3)

Given: BD bisects AC

$$
A B \cong C B
$$

Prove: $\triangle \mathrm{ABD} \cong \triangle C B D$


 $A D \cong B D$
Prove: $\triangle A D E \cong \triangle B D C$

$$
\begin{aligned}
& \text { (1) } \overline{A D} \text { bis. } \overline{C E} \\
& \text { (2) } \overline{C D} \cong \overline{E D}
\end{aligned}
$$

(3) $\overline{A D} \cong \overline{B D}$

(2) If a bes. bis another ses., then it $\div$ into $2 \cong$ seq.
(4) $\angle A D E \cong \angle B D C$
(4) Vertical $\angle s$ are $\cong$
(5) $\triangle A D E \cong B D C$
(5) SAS (ster 2,4,3)

