

3.4. Advanced Algebra Linear Programming

DATE: 11/19

Target 3A. Translate a verbal model into an algebraic model

Target 3D. Graph a system of inequalities to determine the feasible region and maximize or minimize the objective function

Target 3E. Problem solve using Linear Programming

Problem

A shoe company produces Air Jordan's and regular Nike sporting shoes. Long-term projections indicate an expected demand of ^① at least 100 Nikes and 80 Air Jordan's each day. Because of limitations on production capacity ^②, no more than 200 Nikes and 170 Jordan's can be made daily. To satisfy a shipping contract ^③ a total of at least 200 shoes must be shipped each day.

See step 5

If each Nike sold results in a \$2 loss, but each Air Jordan produces a \$5 profit, how many of each type should be made daily to maximize net profits?

Step 1: Define the variables.

Hint: Variables are defined using the question.

Let n be the # of NIKE shoes

Let j be the # of Jordan shoes

Step 2: Write a system of inequalities.

Hardest part!

① $n \geq 100, j \geq 80$

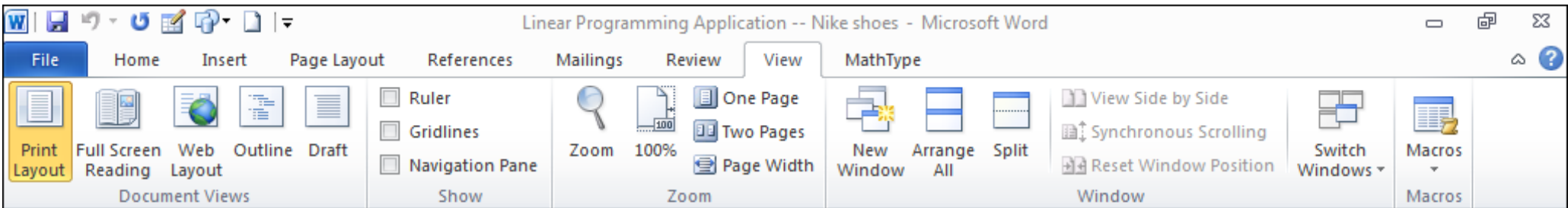
↓ at least

② $n \leq 200, j \leq 170$

↓ no more than

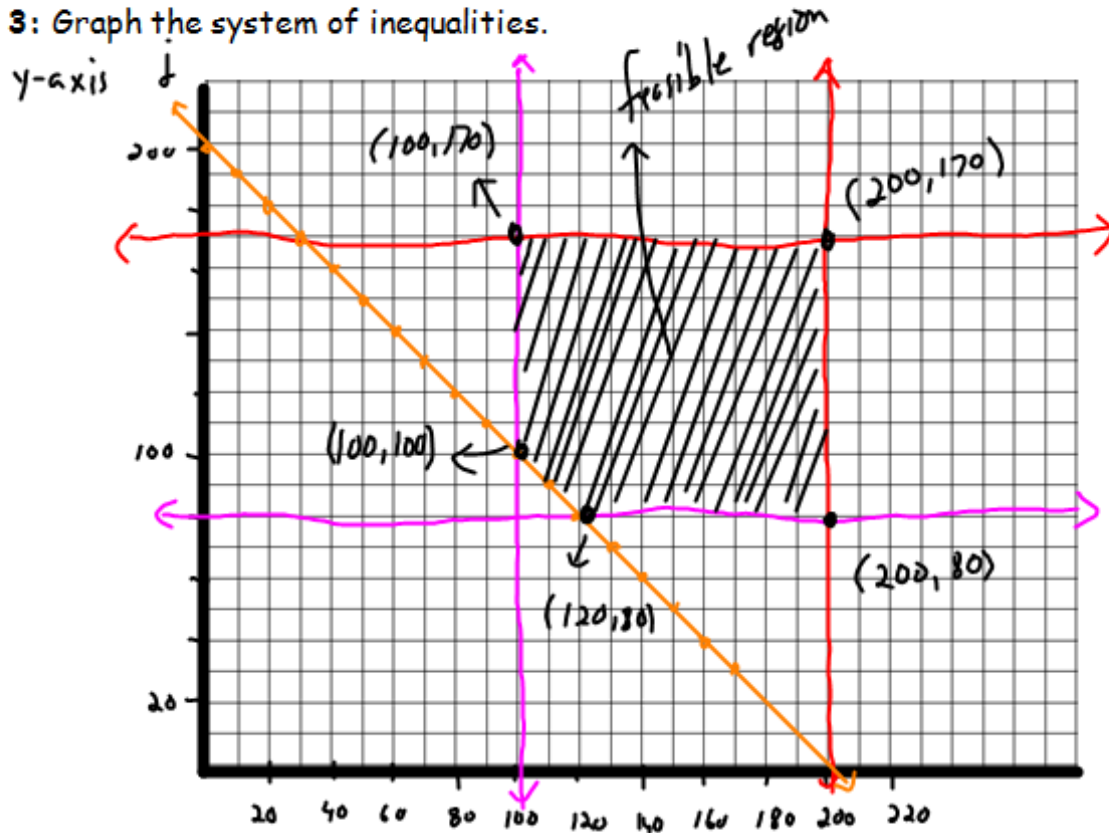
③ $n + j \geq 200$

↓ no more than



Step 3: Graph the system of inequalities.

All lines Solid!



$n \geq 100$ Shade \uparrow or \rightarrow
 $j \geq 80$ shade \uparrow
 $n \leq 200$ Shade \downarrow or \leftarrow
 $j \leq 170$ shade \downarrow
 $n + j < 200$
 $-n \quad -n$
 $j < -1n + 200$
 Slope: $-\frac{1}{1} = -\frac{10}{10} \downarrow$
 $y - 1n = 200$
 x-axis shade \uparrow

Step 4: Find the coordinates of the vertices of the feasible region.

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Step 4: Find the coordinates of the vertices of the feasible region.

The coordinates are:

1. (200, 80)
2. (200, 170)
3. (120, 80)
4. (100, 100)
5. (100, 170)

Step 5: Write a function to be maximized or minimized.

$$P(n, j) = -2n + 5j$$

↓
negative
means loss

Step 6: Substitute the coordinates of the vertices into the function.

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Step 6: Substitute the coordinates of the vertices into the function.

Use function $P(n, j) = -2n + 5j$

$(200, 80) : -2(200) + 5(80) = 0$

$(200, 170) : -2(200) + 5(170) = 450$

$(120, 80) : -2(120) + 5(80) = 160$

$(100, 100) : -2(100) + 5(100) = 300$

$(100, 170) : -2(100) + 5(170) = 650$

Step 7: Select the greatest or least result. Answer the problem.

The greatest result is

To max. profit, make
100 Nikes & 170 Jordans
each day! Phen... \Downarrow