Name:
Period: $\qquad$
Honors Advanced Algebra
Study Guide Key Concept 2-Polynomials
Use the given functions to perform the operations.

$$
h(x)=3 x-4 \quad g(x)=-2 x^{2}+7 x-8 \quad f(x)=8-3 i \quad b(x)=12-i \quad d(x)=-3+4 i
$$

1) Find $(h-g)(x)$
2) Find $(h \cdot g)(x)$
3) Find $(f+2 b-d)(x)$

Write the following in standard form.
4) $(3-8 i)^{2}$

Determine the factors of the graphed polynomial
5)


Create a polynomial of least degree in factored form using the information given below.
6) $x=8 \quad x=-6 \quad x=-13$
7) $x=-2 \quad x=-9 i$

Solve using algebra AND check your work using a graphing calculator.
8) $x^{3}-81 x=0$
9) $2 x^{3}+20 x^{2}=48 x$
10) You know that $2 x^{3}-17 x^{2}+19 x+14$ has a factor of $(x-2)$. What are the other two factors?
11) Multiplying $(x+4)$ by what quadratic expression gives us $x^{3}-2 x^{2}-15 x+36 ?$
12) Zeros: $\{-5,-1,7\}$

Min of $y=-8$ at $(-3,-8)$
Max of $y=4$ at $(3,4)$

13) Factors: $(x+4), x,(x-6)$

Min of $y=-5$ at $(3,-5)$
Max of $y=7$ at $(-2,7)$


## relative min and relative max

14) 

| $x$ | $f(x)$ |
| :---: | :---: |
| -6 | -27 |
| -5 | 0 |
| -4 | 7 |
| -3 | 0 |
| -2 | -15 |
| -1 | -32 |
| 0 | -45 |
| 1 | -48 |
| 2 | -35 |
| 3 | 0 |
| 4 | 63 |
| 5 | 160 |

Describe the end behavior in limit notation. Also state the domain and range.
15) $f(x)=x^{3}-3 x+2$
16) $g(x)=-x^{3}+x^{2}+5 x+1$
$\lim f(x)=$
$\lim f(x)=$
$x \rightarrow-\infty$
$\lim f(x)=$ $x \rightarrow \infty$

$$
\lim _{x \rightarrow \infty} f(x)=
$$

17) $d(x)=x^{4}+x^{3}-4 x^{2}+5$
18) $h(x)=-x^{4}+4 x^{2}+3 x-4$
$\lim f(x)=$ $x \rightarrow-\infty$

$$
\lim f(x)=
$$

$$
x \rightarrow \infty
$$

$\lim _{x \rightarrow-\infty} f(x)=$
$\lim f(x)=$ $x \rightarrow \infty$

Domain:
Range:

Domain:
Range:
Domain:
Range:

Domain:
Range:
19). The height of a box is 3 cm less than the width. The length is 2 cm less than the width. The volume is 50 cm cubed. What is the width of the box? Also determine the height and length.
20) A box has the dimensions of $x, 10-2 x$, and $12-2 x$. Find the maximum value of the box and the value of $x$ that generates that volume.
A) $14 x^{2}-7 x$
B). $x^{2}-36$
C) $x^{2}+16$
D) $x^{2}-5 x-36$
E). $2 x^{2}+3 x-20$

