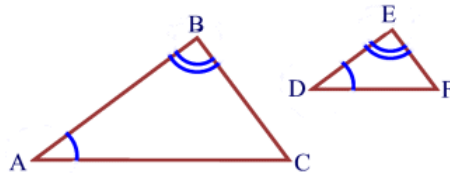


7C – Similarity

❖ Vocabulary, Formulas, Theories:

- **Similar Figures:** figures that are the same shape but not necessarily the same size.
- **Scale Factor:** the ratio of corresponding sides of similar figures.
- **Angle Angle Similarity (AA~):** If two angles of one triangles are congruent to two angles of another triangle, the triangles are similar.

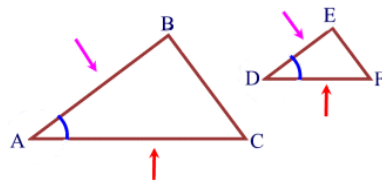


$$\text{If: } \angle A \cong \angle D$$

$$\angle B \cong \angle E$$

$$\text{Then: } \triangle ABC \sim \triangle DEF$$

- **Side Angle Side Similarity (SAS~):** If an angle of one triangle is congruent to the corresponding angle of another triangle and the length of the sides including these angles are in proportion, the triangles are similar.

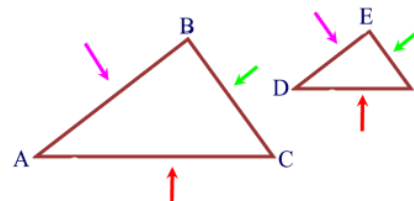


$$\text{If: } \angle A \cong \angle D$$

$$\frac{AB}{DE} = \frac{AC}{DF}$$

$$\text{Then: } \triangle ABC \sim \triangle DEF$$

- **Side Side Side Similarity (SSS~):** If the three sets of corresponding sides of two triangles are in proportion, the triangles are similar.

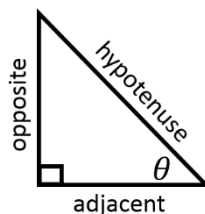


$$\text{If: } \frac{AB}{DE} = \frac{AC}{DF} = \frac{BC}{EF}$$

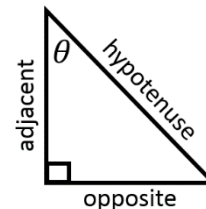
$$\text{Then: } \triangle ABC \sim \triangle DEF$$

- **Trigonometric Ratios:** ratios that are created using trigonometric functions and a right triangle.

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}} \quad \cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}} \quad \tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$



- The "opposite" side and "adjacent" side depend on the location of the angle.
- The hypotenuse is always across from the 90 degree angle.



- **SOHCAHTOA:** a term used to help recall how to set up trigonometric ratios.

SOHCAHTOA

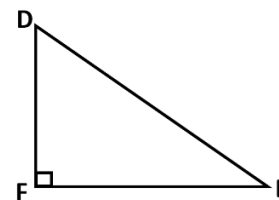
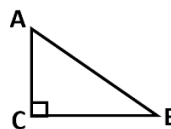
Soh Cah Toa

$$S = \frac{o}{h} \quad C = \frac{a}{h} \quad T = \frac{o}{a}$$

$$\sin \theta = \frac{\text{Opp}}{\text{Hyp}} \quad \cos \theta = \frac{\text{Adj}}{\text{Hyp}} \quad \tan \theta = \frac{\text{Opp}}{\text{Adj}}$$

Video - "Trigonometric Ratios and Similarity - Example 1" - MathontheWeb (7:35)

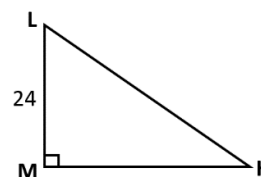
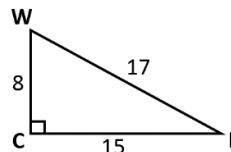
EX1) If $\triangle ABC \sim \triangle DEF$, choose the expression that is equivalent to $\cos(A)$: Is it $\sin(D)$ or $\sin(E)$? Explain.



EX2) Use $\triangle WCE \sim \triangle LMH$ to determine the value of the trigonometric expressions.

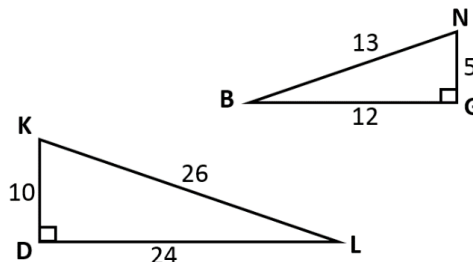
a) $\cos(L)$

b) $\cos(H)$

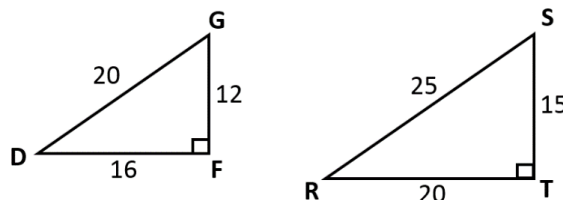


Video - "Trigonometric Ratios and Similarity - Example 2" - MathontheWeb (16:02)

EX3) Find the cosine ratios of the corresponding non-right angles for $\triangle KDL$ and $\triangle NGB$. Compare the ratios to draw a conclusion.



EX4) Prove that $\cos(G)$ and $\cos(S)$ are equivalent.



EX5) Solve for the missing variables and determine if $\cos(\angle DEA) = \cos(\angle CBA)$.

